Comparison of Clustering Algorithms for Learning Analytics with Educational Datasets

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Received 3 November 2017 | Accepted 22 January 2018 | Published 9 February 2018



ABSTRACT

Learning Analytics is becoming a key tool for the analysis and improvement of digital education processes, and its potential benefit grows with the size of the student cohorts generating data. In the context of Open Education, the potentially massive student cohorts and the global audience represent a great opportunity for significant analyses and breakthroughs in the field of learning analytics. However, these potentially huge datasets require proper analysis techniques, and different algorithms, tools and approaches may perform better in this specific context. In this work, we compare different clustering algorithms using an educational dataset. We start by identifying the most relevant algorithms in Learning Analytics and benchmark them to determine, according to internal validation and stability measurements, which algorithms perform better. We analyzed seven algorithms, and determined that K-means and PAM were the best performers among partition algorithms, and DIANA was the best performer among hierarchical algorithms.

KEYWORDS

Clustering Methods, Computer Languages, Data Analysis, Engineering Students, Performance Evaluation, Unsupervised Learning.

DOI: 10.9781/ijimai.2018.02.003

I. Introduction

SINCE the turn of the Century, researchers have been studying clustering methods and comparing them from different perspectives. These algorithms were the core of an emerging data mining discipline, which would soon explode along with the popularity of big data approaches in all fields. And when these ideas were applied to digital education, the field of Learning Analytics was born.

But the core of these approaches is still the use of adequate clustering algorithms for each scenario, and this problem has received a fair share of attention. Berkhin contrasted theoretically different algorithms [1], and indicated how to perform the most typical evaluations, data preparation and measurements. In [2], the authors studied 216 articles written between 2000 and 2011, classifying the literature in three axes (knowledge types, analysis types, and architecture types) and exploring the different context where such techniques may be used. Remarkably, the study highlighted the potential applications of data mining techniques in social sciences, psychology, cognitive sciences and human behavior, which is very relevant for this specific work. In turn, other studies such as [3] provided solid grounds for defining and scoping clustering, discussing aspects such as variable selection and similarity measurements, and provided a theoretical foundation of grouping methods and applications. Other authors have studied the theoretical limitations and potential pitfalls of these techniques [4].

All in all, the theoretical foundation of clustering algorithms is solid and has been the object of detailed studies. In terms of experimental analysis, we can find publications as early as in the 80s. In [5] the

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author proposed specific analysis methods, and also studied the performance impact of different perturbations. In [6] the authors compared five grouping algorithms and used four different supervised automatic learning algorithms to analyze their performance. In [7] three algorithms were measured with four cluster validation indexes, using synthetic and real datasets. Other relevant works have conducted formal tests to determine the most appropriate data mining algorithms for specific fields such as classification [8] or text mining from RSS sources [9]. However, few experimental studies focused on analyzing performance using specifically educational datasets.

In turn, Learning Analytics (LA) research ranges from theoretical essays on the potential impact of LA in education [10] to very focused studies on how it is useful for establishing personalized feedback to improve academic performance [11]. There are also works proposing dynamic models for data analysis of educational datasets [12] or proposing the use of different statistical algorithms to rank academic performance [13]. Regarding the evolution of the state of the art, different works have studied stakeholders, benefits and challenges [14]-[15] or differentiated types of educational settings, tasks and outputs [16]. Other authors have studied specific quality indicators to assess the impact of LA in education [17] or studied in depth the foundations of LA in terms of data mining techniques [18]. All these efforts can be characterized for their use of clustering algorithms as an analysis technique, which is the focus of this work, but typically focus on one or two algorithms at most, or just in the educational and social implications, rather than focusing specifically in experimental comparison of the performance of different algorithms when applied in educational settings.

And while the challenges of small-scale and relatively clean educational datasets lie mostly on how to identify the best visualizations or practical uses of the data, the emergence of open education formats is yielding increasingly complex and noisy datasets, imposing non-

trivial burdens on the data mining algorithms applied to make sense of how students are interacting with these open materials.

At the crossroads of these lines of research, our goal is to contribute experimental validation of the performance of different clustering techniques when specifically applied to educational datasets, thus providing a more solid foundation for further works focusing on practical aspects rather than back-office performance.

To achieve this goal, we have conducted a practical experiment using a real-world dataset provided by Universidad Mariana in Colombia, benchmarking different algorithms and configurations in terms of internal validations and stability measurements.

II. MATERIALS AND METHODS

The experimental design is quite straightforward. We started with a literature review to select a representative set of clustering algorithms. Then, we organized a workflow for testing each algorithm and selected specific measurements for comparison, and finally we applied this workflow to all algorithms targeting an educational dataset provided by Universidad Mariana. This section details each of these steps.

A. Selecting the Algorithms to Be Benchmarked

The specific selection of algorithms was conducted after performing a literature review, with a heavy influence of related works from other fields ([1], [4], [16]) and trying to provide a wide perspective of the potential approaches.

The final selection of algorithms is summarized in Table I.

B. Experimental Platform

We employed different platforms and tools to create our experimental pipeline. We started with raw and cross-referenced data available on an Oracle 10g database server. We extracted different listings and used Microsoft Excel to review, perform basic cleaning (including anonymization) and saving as CSV (comma-separated values) files.

All statistical analyses and clustering algorithms were applied using the opensource platform R, for which we created our test scripts using the R Studio graphical interface. The platform was also used to create the different visualizations that helped in this study and that

TABLE I. ALGORITHM SELECTION

NAME	Description
K-means	It builds the clusters with similarity measure, each cluster is represented by a centroid, which is the average of its elements. It works only with numerical data and its affected by outliers [1].
CLARA	It builds the clusters without all the data, instead, sample them at random and then the centers are calculated with the PAM algorithm. It works with numerical data [1].
PAM	It is a robust version of K-means. The process of grouping is done through the search of a sequence of objects called medoids. Its main characteristic is the reduction of the average dissimilarity of the observations to its nearest observation [1].
FANNY	It calculates the clustering in a diffuse way in a number K clusters.
Hierarchical	It uses previous clusters to form the new clusters. It's of two types: divisive (top-down) and agglomerative (bottom-up). It can be applied with any type of variables and it is not necessary to establish a priori the number of clusters to be formed. It is sensitive to noise and outliers.
AGNES	Hierarchical algorithm of agglomerative type, it uses the Euclidean distance as similarity measure.
DIANA	Hierarchical algorithm of divisive type, it uses the Euclidean distance as similarity measure.

are included in this article. In Table II we provide a summary of the different libraries that we used for the experiment.

C. Benchmarking Performance

In order to benchmark the performance of each algorithm, we focused on the facilities provided by the *clValid* library presented in [19] to measure internal and stability validations.

Internal validations are computed using intrinsic information from the datasets to assess the quality of the resulting clusters. We used the three main internal validation measurements offered by the validation library: *connectivity* (which provides a value in the $[0, \infty)$ range where lower is better), *silhouette width* (which proves values in the (-1,1) range where higher is better), and *Dunn index* (which provides a value in the $[0, \infty)$ range where higher is better).

In terms of stability measurement, we again selected the main measures from [19], all of them focused on inspecting each cluster and sequentially removing internal columns and checking whether the cluster remains valid. We employed APN (average proportion of non-overlap), AD (average distance between measurements), ADM (average distance between means) and FOM (figure of merit, focused on the average intra-cluster variance of the observations). All of them take values in the $[0,\infty)$ range where higher is better except APN, with values in the [0,1] range with preferred results close to zero.

TABLE II. R LIBRARIES

Library	Description
cluster	It allows clustering analysis by implementing hierarchical and partition algorithms. Details in: https://cran.r-project.org/web/packages/cluster/index.html
ggplot2	It builds visualizations using the information of the data meaning. Details in: https://cran.r-project.org/web/packages/ggplot2/index.html
factoextra	It offers different easy-to-use functions to extract and visualize the results of multivariate analyzes, it simplifies clustering analysis and its graphical representations. Details in: https://cran.r-project.org/web/packages/factoextra/index.html
readr	It provides fast and friendly mechanisms to read files in csv, tsv and fwf formats. Details in: https://cran.r-project.org/web/packages/readr/index.html
RColorBrewer	It provides color schemes to be used with various types of graphic representations. Details in: https://cran.r-project.org/web/packages/RColorBrewer/index.html
gplots	It offers several tools to draw processed data. Details in: https://cran.r-project.org/web/packages/gplots/index.html
d3heatmap	It creates interactive heat maps that can be viewed in different environments such as R console and R studio. Details in: https://cran.r-project.org/web/packages/d3heatmap/index.html
stats	It offers different statistical functions for data analysis. Details in: https://stat.ethz.ch/R-manual/R-devel/library/stats/html/00Index.html
NbClust	It provides 30 indexes to determine the optimal number of clusters in a dataset and it offers the best clustering scheme of different results. Details in: https://cran.r-project.org/web/packages/NbClust/
clValid	It provides functions to evaluate clustering results in biological and statistical way. Details in: https://cran.r-project.org/web/packages/clValid/index.html
pvclust	It is an implementation of bootstrap resampling to evaluate the uncertainty in hierarchical clustering. Details in: https://cran.r-project.org/web/packages/pvclust/index.html

D. Preparing the Dataset

One particularity of Learning Analytics approaches is the focus on inspecting academic data generated at specific institutions for specific courses, since comparisons across platforms, institutions and even individual courses may be challenging due to significant differences in usage patterns [10]

We therefore chose to focus on a specific student profile within the host institution: Computer Engineering students enrolled in the first semester with the 2010-2016 timeframe (7 years).

The datasets were constructed with the main measurement of the average grade of all courses in the semester. The data was extracted from the host University's database system, using specific queries and basic data management (e.g. transposing) to create rows representing each specific student's aggregated data.

The scripts were also prepared to provide anonymization when required and removed non-essential personal data (e.g. personal addresses or phone numbers).

All the relevant R scripts as well as the dataset can be downloaded from https://goo.gl/oNHm2R.

III. RESULTS

A. Pre-processing

The first step in our test pipeline was the conduction of relatively simple cleanup tasks, mostly focused on removing instances where some grades were missing (this may happen either due to an administrative issue or an error in the grade reporting system).

After this step, we analyzed for each variable different comparison statistics, averaging their maximum, minimum, average and mean values. We determined that their standard deviation and variances were minimal, therefore making it possible to work directly with the original data without requiring a previous normalization.

We also analyzed the dataset to validate its clusterability, using two approaches: first, we used the *Hopkins statistic* method from [20], with a resulting value of 0.2036606 (<0.5) which shows that the values are potentially groupable. We also validated this notion visually, by representing the tendency of the data to be grouped. This is achieved by (1) calculating the dissimilarities between all datapoints and storing them in a dissimilarity matrix according to their Euclidean distances, (2) sorting the matrix so that similar objects are closer together and (3) displaying the matrix to check the presence of high values along the diagonal of the matrix (Fig. 1).

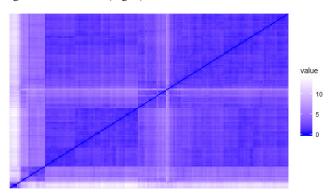


Fig. 1. Data clustering trend where we can observe dark blue rectangles aligned with the diagonal line, which can be interpreted as a potential clustering amenability of the data.

Therefore, we could ascertain the adequacy of our dataset for the goals of our experiment.

B. Optimal K Value

In order to determine the optimal number of clusters, we again used to separate and complementary methods. The first approach we used employed the *gap stastic* [21] targeting the K-means algorithm with a maximum value of K=10 and 10,000 Monte Carlo samples. The result can be observed in Fig. 2, yielding a proposal for one single cluster (or rather hinting that the data was not prone to clustering), although applying the *1-standard error* criterion K=5 may also be a valid candidate.

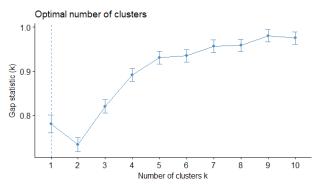


Fig. 2. Optimal K presented by the gap statistic.

Given this partially unsatisfactory result, we also looked at the nbClust R package, which analyses 30 separate indexed to determine the optimal K. We ran this analysis for values of K in the [2,10] range, with full clustering and all indexes included. As observed in Fig. 3, this yielded an optimal number of clusters of K=3.

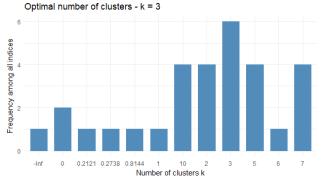


Fig. 3. Optimal K reported by nbClust.

C. Algorithm Execution with Optimal K Value

All seven algorithms were run on the data using K=3 in order to study their behavior and performance.

Regarding the set of partition algorithms, Fig. 4a shows the dispersion and cluster charts produce by the K-means, CLARA and PAM algorithms (all three produced the same output), while Fig. 4b shows the results for the FANNY algorithm, which displayed a significantly worse performance.

These results were validated through a silhouette inspection, which measures the adequacy of each observation for each cluster representing the average distance between groups. Fig. 5 shows the results of these inspections. The K-means, CLARA and PAM algorithms yielded an average silhouette width of 0.55 while the FANNY algorithm yielded 0.29. This indicates a good result for the first three algorithms, while the FANNY algorithm even had a cluster with negative average width, representing a large number of incorrectly assigned instances.

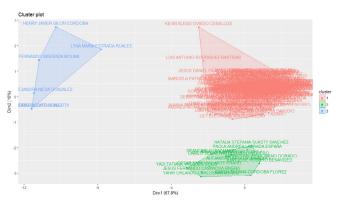


Fig. 4 a. Cluster plot for K-means, CLARA and PAM algorithms. All three yielded the same result.

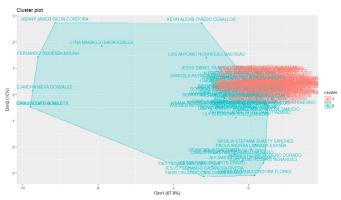


Fig. 4 b. Cluster plot for the FANNY algorithm.

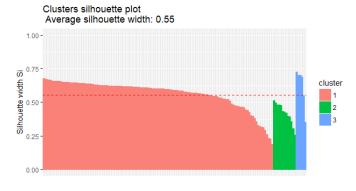


Fig. 5 a. Clusters silhouette plot for the K-means, CLARA and PAM algorithms. All observations are >0 with an average of 0.55.

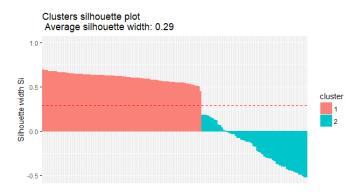


Fig. 5 b. Clusters silhouette plot for the FANNY algorithm. In cluster 2 (cyan color) there are negative values.

We took the same approach for our selection of hierarchical algorithms. Fig. 6 show the cluster plots for the hierarchical and AGNES algorithms (which were equal) and for the DIANA algorithm (which presented issues with one of the clusters).

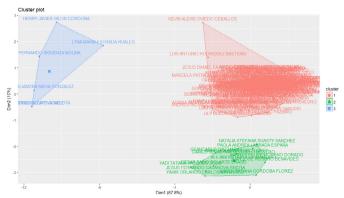


Fig. 6 a. Cluster plot for the hierarchical and AGNES algorithms. Both yielded the same result.

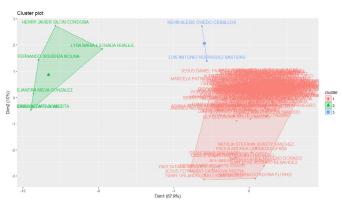


Fig. 6 b. Cluster plot for the DIANA algorithm.

Similarly to the other family, the clusters yielded by the hierarchical variants were validated through silhouette inspection, using a different visualization due to concerns with the very small cluster yielded by the DIANA algorithm.

The silhouettes can be observed in Fig. 7. The first two algorithms yielded the same result while, remarkably, the DIANA algorithm had produced three clusters, all with positive silhouette values, meaning that all values are well assigned, even if the value for cluster #3 (the small blue one in Fig. 6b) is relatively low (0.27) although the overall value is 0.54, very close to the other two algorithms.

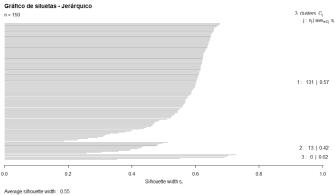


Fig. 7 a. Clusters silhouette plot for the hierarchical and AGNES algorithms.

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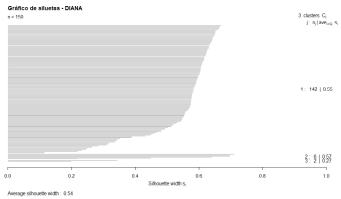


Fig. 7 b. Clusters silhouette plot for the DIANA algorithm.

D. Algorithm Execution Doubling the Optimal K Value

While the previous observations already present some interesting insights, the decision of going with a specific K value was a concern, especially given that one of our tests suggested potential gains for relatively high K values.

We therefore repeated the process using a higher value, K=6 (doubling the previous value) in order to check both the consistency of the previous results and the effect of increasing K in general.

In Fig. 8 we can observe the performance of the clustering algorithms once we double the K value. FANNY basically maintains the same average (and poor) performance for K=3 and K=6, while the other algorithms actually decreased their performance, yielding small but significant errors in most cases. In this sense, PAM and CLARA took a significant performance hit, with 11 and 10 wrongly classified observations respectively. In turn, the classic K-means algorithm presented four negative values after increasing the K value.

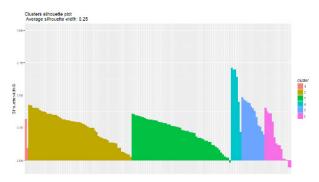


Fig. 8 a. Clusters silhouette plot for K-means with K=6.

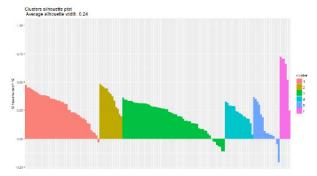


Fig. 8 b. Cluster silhouette plot for CLARA with K=6.

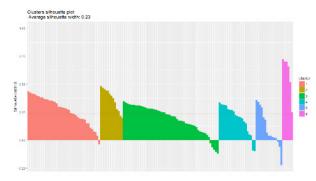


Fig. 8 c. Cluster silhouette plot for PAM with K=6.

Regarding hierarchical algorithms, their cluster silhouette plots (Fig. 9) show that the hierarchical and AGNES algorithms still show the same behavior but doubling the K value impacted their performance negatively. Not only they assigned more instances incorrectly, but they also reduced the average silhouette value from 54% to 24%. In turn, the DIANA algorithm also took a performance hit, but did not experience any incorrect classifications.

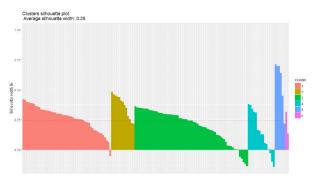


Fig. 9 a. Cluster silhouette plot for hierarchical with K=6.

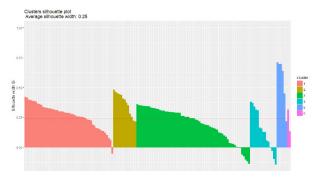


Fig. 9 b. Cluster silhouette plot for AGNES with K=6.

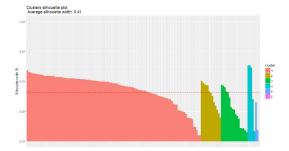


Fig. 9 c. Cluster silhouette plot for DIANA with K=6.

E. Internal Validation and Stability Measurement

As stated in previous section, in order to assess the performance of the different algorithms we performed a comparison using internal validation and stability measurements. Fig. 10 displays the R output with all the internal validation scores for our selection of algorithms, for varying K values from 3 to 6, while Fig. 11 displays the output for stability scores.

```
Clustering Methods:
kmeans clara pam fanny hierarchical agnes diana
cluster sizes:
Validation Measures:
              Connectivity
                               5.7167 11.1667
                                                32,6063 38,1222
kmeans
                               0.3721
                                        0.3721
                                                 0.1034
                                                          0.2010
              Silhouette
                               0.5549
5.7167
                                        0.5476
                                                 0.4209
                                                          0.3849
                                       54.1635
                                                70.5667
                                                         69.2286
clara
              Connectivity
                               0.3721
                                                 0.0494
                               0.5549
5.7167
                                                0.2301
75.7325
              Silhouette
                                        0.2151
                                                          0.2435
                                       58.4603
              Connectivity
                                                         76.1421
pam
                                        0.0485
                                                 0.0485
              Silhouette
                               0.5549
                                        0.2168
                                                 0.2262
                                                          0.2345
fanny
              Connectivity
                                   NA
                                             NΑ
              Silhouette
                                   NΑ
                                             NΑ
                                                      NA
                               8.6151 11.9484 13.7079 16.6579
hierarchical
              Connectivity
                               0.3883
                                        0.3883
                                                 0.4338
                                                          0.4338
              Silhouette
                               0.5450
                                        0.5377
                                                 0.5513
                                                          0.5524
                               8.6151 11.9484
                                                13.7079
agnes
              Connectivity
                                                         16.6579
                                                 0.4338
                               0.3883
                                        0.3883
                                                          0.4338
              Silhouette
                               0.5450
                                        0.5377
                                                 0.5513
                                                          0.5524
                               8.6151 10.3746
diana
              Connectivity
                                                28.6325
                                                         31.9659
                                                 0.1209
                               0.3883
                                        0.4338
              Dunn
              Silhouette
                                        0.5586
                               0.5450
                                                 0.4156
                                                          0.4083
Optimal Scores:
              Score Method
5.7167 kmeans
                                     Clusters
Connectivity
              0.4338 hierarchical
Silhouette
              0.5586 diana
         Fig. 10. Internal validation scores for all algorithms.
        Clustering Methods:
         kmeans clara pam fanny hierarchical agnes dia
        cluster sizes:
         3 4 5 6
        Validation Measures:
                                                  5
                                                         6
                                                   0.0345
                       APN
                            0.0350 0.1462 0.0524
                       AD
                            2.4473 2.4391
                                           2.2072
                                                   2.0718
                            0.2036 0.5720
                                           0.4537
                                                   0.3029
                       ADM
                            0.6958 0.6866 0.6907
                                                   0.6690
                                           0.1661
        clara
                       APN
                            0.0758 0.1308
                                                   0.1674
                       AD
                       ADM
                            0.2482 0.3520 0.4425
                                                   0.5323
                            0.6917 0.6630
                                           0.6674
                                                   0.6680
                       FOM
                                           0.1706
                            0.0476 0.1499
                       AD
                            2,4014 2,2172
                                           2.0254
                                                   1.9934
                            0.1323 0.4477
                                            0.3421
                       ADM
                                                   0.5667
                       FOM
                            0.6957 0.6676 0.6585 0.6578
        fanny
                       APN
                                NA
                                        NA
                                                NA
                       AD
                       ADM
                                 NA
                                        NA
                                                NA
                                                        NA
                       FOM
                                           0.0049 0.0071
2.2709 2.2316
        hierarchical
                       APN
                            0.0187 0.0525
                            2.7104 2.6614
                       AD
                       ADM
                            0.1080 0.2569
                            0.7016 0.6912
0.0187 0.0525
                                           0.6787
                                                   0.6715
                       FOM
        agnes
                       APN
                                           0.0049
                                                   0.0071
                            2.7104 2.6614
                                              2709
                       AD
                       ADM
                            0.1080 0.2569
                                           0.1111
                                                   0.1171
                       FOM
                            0.7016 0.6912
                                            0.6787
                                                   0.6715
        diana
                       APN
                            0.0350 0.0265
                                           0.0176 0.0161
                            2.7106 2.3175
                       AD
                                           2.2031 2.0415
                            0.1729 0.1330 0.4379 0.1834
                       FOM
                            0.7015 0.6873 0.6765 0.6598
        Optimal Scores:
                                   Clusters
        APN 0.0049 hierarchical
            1.9934 pam
        AD
```

Fig. 11. Stability scores for all algorithms.

0.1080 hierarchical

FOM 0.6578 pam

Regarding partition algorithms, for K=3, K-means, CLARA and PAM tie as the best performers, due to their lower connectivity score (5.7167), best silhouette coefficient (0.5549) and best Dunn index (0.3721). However, this tie disappeared when we increased K values, with K-means maintaining better performance while CLARA and PAM quickly degraded their numbers. In turn, the FANNY algorithm yields no output given its inability to generate measurable clusters. In terms of stability, PAM achieved the best score with K=6 for AD and FOM measurements, and also performed excellently with ADM with K=3. K-means achieved the best APN score with K=6.

Focusing on hierarchical algorithms, hierarchical achieved the best connectivity and Dunn scores for K=3 and K=5 respectively, while DIANA achieved the best score in terms of correct instance assignments when K=4. In terms of stability scores, hierarchical again displays the best scores for K=3 and K=5 for APN and ADM measurements, while DIANA achieves optimal values for AD and FOM when K=6.

IV. DISCUSSION

One of the most relevant (although reasonably expected) observations is that no algorithm is a clear and obvious winner across all measurements and potential K values.

In terms of internal validation, K-means, CLARA and PAM achieved the best overall scores with K=3, although CLARA and PAM experienced a worst degradation as the K value increased. However, the hierarchical and AGENS algorithms also achieve very significant Dunn scores when K=4.

If we focus on K=3 (our selected optimal value), the worst performers in connectivity were the three hierarchical algorithms, although they achieved better Dunn index scores. However, they also presented more incorrect assignments, and therefore can be considered worst performers overall.

However, as we increased the K value, partition algorithms degraded their performance quickly, while hierarchical algorithms remained more stable and actually improved some scores.

In terms of stability, again there is no single algorithm that achieves the best score in all four measurements. PAM exhibited good AP and FOM behavior at K=6, hierarchical achieved very good APN with K=5 and very good ADM with K=3.

Again, if we focus on K=3, the worst performer in terms of APN and ADM was CLARA, while DIANA and AGNES performed poorly in AD and FOM respectively.

The pattern of degradation as we increased the K value exhibited by partition algorithms was also apparent when looking at stability measurements, yielding a consistent conclusion of the better behavior of hierarchical algorithms for higher number of clusters.

The FANNY algorithm failed to produce significant clusters and was therefore deemed as poorly fit for our specific dataset.

V. CONCLUSION AND FUTURE WORKS

Open education is bound to push the boundaries of how we analyze our educational datasets. And as the scope of our research actions Learning Analytics becomes more and more specialized, the specific underlying techniques, including the selection of a particular clustering algorithm, are bound to receive less attention than appropriate.

This study aims to provide researchers with insights into how the different algorithms exhibit different performance patterns depending on specific measurements and variation in K values, especially when the dataset is highly driven by a set of grades in different courses.

This is achieved through a detailed and highly practical experiment,

selecting the most prominent algorithms identified in the literature and analyzing them using an assortment of assessment tools and an educational dataset from a higher education institution.

Among the seven clustering algorithms selected, we measured which algorithms performed better at an experimentally determined K value (K=3) and henceforth how they changed their performance if we increased this number.

During the experimental work we highlighted different relevant observations, from which we can distil some specific insights:

- Among partition algorithms, K-means and PAM were the best performers overall. The former achieved the best results in terms of internal validation (especially as we increased the K value) while the latter performed better in terms of stability.
- Among hierarchical algorithms, DIANA and hierarchical were the best performers, with a similar variation: the former achieved better internal validation scores, while the latter achieved better stability scores.
- Student grades in the sample dataset were highly groupable, as corroborated by the Hopkins statistic, a result that we expect would be extrapolated to other educational datasets, especially in higher education, where students tend to form grade patterns with ease. In lower education levels, the breadth of topics may introduce additional noise as students may have greater affinities for specific courses.
- In terms of determining the optimal K value, the Gap statistic was not really helpful, suggesting one single cluster even though the performance of the clustering algorithms for higher K values was rapidly apparent.
- Increasing the K value improved the performance of many algorithms in most metrics, although the number of errors also increased, and this improvement should be taken in context.

This work, however, also has specific limitations. Firstly, the preparation of the dataset was performed through an aggressive cleanup of the data, discarding all instances where any piece of information was missing. This resulted in a clean dataset 44% smaller than the original one. Given that this was an official dataset provided by the host University, it is to be expected to get similar noise levels in other real (non-synthetic) datasets, and better data cleanup techniques could be required. Making sure that we do not loose significant information while cleaning up data remains a significant open line of research.

In addition, most validations were performed trough different variations of Euclidean distance measurements, ignoring other approaches that may provide additional insights. This invites the potential expansion of this experiment either by including new measurements or by testing alternative educational datasets (or both).

Finally, we expect that the comparisons performed in this work will be helpful for future researchers looking into how to select the best algorithms for performing clustering analysis of educational datasets in higher education.

Further than the specific scores achieved by the different algorithms, we believe that this work adds value by identifying performance patterns that can be used as a base in future research.

ACKNOWLEDGMENT

This work was partially funded by Universidad Internacional de La Rioja (UNIR, http://www.unir.net) through the Research Institute for Innovation & Technology in Education (UNIR iTED, http://ited.unir.net) and the IBM-UNIR Chair on Data Science in Education.

Thanks to Universidad Mariana - Pasto - Colombia for their collaboration in this research, especially to Iván Bastidas for his help in obtaining the data for this experiment.

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